

A Tableau Based Decision Procedure for an Expressive Fragment of Hybrid Logic with Binders, Converse and Global Modalities

Serenella Cerrito · Marta Cialdea Mayer

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Abstract In this paper we provide the first (as far as we know) direct calculus deciding satisfiability of formulae in negation normal form in the fragment of FHL (full hybrid logic with the binder, including the global and converse modalities), where no occurrence of a universal operator is in the scope of a binder. By means of a satisfiability preserving translation of formulae, the calculus can be turned into a satisfiability decision procedure for the fragment $FHL \setminus \Box \downarrow \Box$, i.e. formulae in negation normal form where no occurrence of the binder is both in the scope of and contains in its scope a universal operator. The calculus is based on tableaux and termination is achieved by means of a form of anywhere blocking with indirect blocking. Direct blocking is a relation between nodes in a tableau branch, holding whenever the respective labels (formulae) are equal up to (a proper form of) nominal renaming. Indirect blocking is based on a partial order on the nodes of a tableau branch, which arranges them into a tree-like structure.

Keywords Automated reasoning · Tableaux · Modal logic · Hybrid logic

1 Introduction

Hybrid logic is an extension of modal (propositional, possibly multi-modal) logic K by means of three constructs: *nominals* (propositions which hold in exactly one state of the model), the *satisfaction operator* @ (allowing one to state that a given formula holds at the state named by a given nominal), and the *binder* \downarrow ,

S. Cerrito (✉)
Lab. Ibisc, Université d'Evry Val d'Essonne, Evry, France
e-mail: serena@ibisc.univ-evry.fr

M. Cialdea Mayer (✉)
Dipartimento di Informatica e Automazione, Università di Roma Tre, Rome, Italy
e-mail: cialdea@dia.uniroma3.it