

# Does accelerating Universe permit varying speed of light?

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**Abstract** We investigate the possible variation of  $c$  in the context of the present accelerating Universe as discovered through SN Ia observations and show that variability of  $c$  is not permitted under the variable  $\Lambda$  models.

**Keywords** General relativity · Dark energy · Varying velocity of light

## 1 Introduction

Historically, the prominent inception of the idea of changing speed of light is due to Thomson and Tait (1874). Earlier Michell (1784) showed that a particular mass to radius ratio of a star implies that the escape velocity of the star would be equal to the speed of light. Contrary to Eddington (1946) a changing speed of light was also not unpleasant to Einstein (1911). However, in the 1930s, variation of  $c$  came in the picture through the alternative explanation of cosmological redshift (Stewart 1931; Buc 1932; Wold 1935).

Recently proposed varying speed of light (VSL) theories (Moffat 1993; Barrow and Magueijo 1998; Albrecht and

Magueijo 1999; Magueijo 2000; Moffat 2002) consider the idea of phase transition to solve the horizon problem and other associated aspects of the Big Bang model. On the other hand, via the relation  $\alpha = e^2/hc$  (where  $e$  is the charge of a proton and  $h$  is Planck's constant), variability of  $\alpha$  implies variability of  $c$  provided constancy of  $e$  and  $h$  is assumed (Webb et al. 1999; Murphy et al. 2001). In dilaton theories also variation of  $c$  have been assumed by several investigators (Bekenstein 1982; Olive and Pospelov 2002; Sandvik et al. 2002).

Under this background, in this small note we have presented our analytical investigation of the possible variation of  $c$  in the context of the accelerating Universe (Perlmutter et al. 1998; Riess et al. 1998).

## 2 The field equations and their solutions

A major problem with the variation of light speed is the violation of energy-conservation law of special theory of relativity, viz.  $E = mc^2$ , where  $c$  being the velocity of light quanta photon in vacua is a constant. To avoid this problem the Einstein field equation

$$G_{ij} = \frac{8\pi G}{c^4} T_{ij} \quad (1)$$

can be written as (Farrell and Dunning-Davies 2007)

$$G_{ij} = \frac{8\pi Gm}{c^2}, \quad (2)$$

by assuming the energy component of  $T_{ij}$  as  $mc^2$ . Therefore, for any departure from  $\Omega \neq 1$ , the speed of light and the curvature term will adjust themselves so as to make the Universe flat.

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