



Embedding locally inverse semigroups into Rees matrix semigroups

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Abstract

We give a necessary and sufficient condition for a locally inverse semigroup to be embeddable into a Rees matrix semigroup over a generalized inverse semigroup.

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1 Introduction

For the standard notions and notation in semigroup theory the reader is referred to [1]. In particular the set of idempotents of a semigroup S will be denoted by $E(S)$, the set of inverses of an element $s \in S$ by $V(s)$. For nonempty subsets $H, K \subseteq S$, HK denotes the usual product of subsets.

Definition 1.1. A regular semigroup is called locally inverse if the submonoid eSe is an inverse subsemigroup of S , for all $e \in E(S)$. If in addition $E(S)$ is a subsemigroup of S , then S is called a generalized inverse semigroup. In this case $E(S)$ is a normal band, i.e. an idempotent semigroup satisfying the equation $xyzx = xzyx$.

Definition 1.2. On a regular semigroup S , a partial order relation $\leq$ is defined by $s \leq t$, if $s = et = tf$, for some $e, f \in E(S)$. It is called the natural partial order. A regular semigroup is locally inverse, if and only if the natural partial order is compatible with the multiplication.

Definition 1.3. An order ideal H of a regular semigroup S , is a nonempty subset H of S , such that $x \leq h$ implies $x \in H$, for all $h \in H$. For $s \in S$ we shall use the notation $[s] = \{x \in S : x \leq s\}$. In any locally inverse semigroup S the equality $[s][t] = [st]$ holds, for all $s, t \in S$.

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