



A Genetic Algorithm For Finding The Semi-Obnoxious (k, l) -core Of A Network

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Abstract

Let $G = (V, E)$ be a graph, with $|V| = n$. A (k, l) -core of G is a subtree with at most k leaves and with a diameter of at most l which the sum of the distances from all vertices to this subtree is minimized. In this paper, we present a genetic algorithm for finding the (k, l) -core of a graph with pos/neg weight.

Keywords: Core, Genetic algorithm, Median subtree, Semi-obnoxious

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1 Introduction

The core of a graph is defined in [6] as a path in the graph minimizing the sum of the distances of all vertices of the graph from the path. This problem is extended to finding a core of specified size l on tree networks in [2, 5, 7]. Peng et al. [8] considered problem with a constraint on numbers of leaves and presented an algorithm for constructing a k -tree core on trees which has time complexity of $O(kn)$. After that, problem is extended to finding a subtree of tree with at most k leaves and with a diameter of at most l so that the sum of the weighted distances from all vertices to the subtree is minimized. This subtree is called a (k, l) -core of tree. Becker et al. [3] presented an efficient algorithm for finding a (k, l) -core of a tree with time complexity of $O(n^2 \log n)$.

If some of the vertices have positive weights and some negative weights the problem is referred to as the semi-obnoxious location problem. Burkard and Krarup [4] showed that the positive or negative (for simplicity we write pos/neg) 1-median, problem on a cactus can be solved in linear time.

Many genetic algorithms are applied to solve some location problems such as median problem and hub location problem[1].

In this paper, we consider (k, l) -core of G that is a subtree with at most k leaves and with a diameter of at most l which the sum of the distances from all vertices to this subtree is minimized. Then present a genetic algorithm for finding the (k, l) -core of a graph with pos/neg weight.

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