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## Extremum seeking control and its application to process and reaction systems: A survey

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## Abstract

The objective of this paper is to present a survey on extremum seeking control methods and their applications to process and reaction systems. Two important classes of extremum seeking control approaches are considered: perturbation-based and model-based methods.

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## 1. Introduction

Most adaptive control schemes documented in the literature [14–16,19] are developed for regulation to known setpoints or tracking known reference trajectories. Yet in some applications the control objective could be to optimize an objective function which can be a function of unknown parameters, or to select the desired states to keep a performance function at its extremum value. Self-optimizing control and extremum seeking control are two methods to handle these kinds of optimization problems. The goal of self-optimizing control is to find a set of controller variables which, when kept at constant set points, indirectly lead to near-optimal operation with acceptable loss [23,26]. The task of extremum seeking is to find the operating set-points that maximize or minimize an objective function. Since the early research work on extremum control in the 1920s [20], many successful applications of extremum control approaches have been reported, for example, fuel flow control to achieve maximum pressure [29], combustion process control for IC engines and gas furnaces [1,25], and anti-lock braking system control [6].

Real-time optimization has seen a resurgence of interest in the recent years. The traditional approach is the modelbased repeated optimization where the model is adapted using the available measurements and numerical optimization is performed on the updated model [34]. An alternative approach is known as extremum seeking. Extremum seeking control allows the solution of the optimization problem as a *control problem* with the advantages related to sensitivity reduction and disturbance rejection.

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